ALLOMETRIC ANALYSIS OF BODY AND WING DIMENSIONS OF **MALE ANISOPTERA**

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Several body dimensions were measured in ²⁹ spp. The relationship between pairs of dimensions was determined by allometric analysis. In general, the wings of dragonflies become relatively longer and narrower as body mass increases; fliers have longer but thinner wings than perchers of comparable size. These trends are probably the result of differences in energetic and structural requirements in flight. Thoracic diameter and volume increase more rapidly than expected as thoracic mass increases and are relatively greater in fliers than in perchers. Thoracic dimensions are partly determined by increased selection for insulating, sub-cuticular air sacs in large fliers.

INTRODUCTION

Since its introduction by HUXLEY (1932), allometric analysis has been used widely in studies of the dimensional relationships of animals (GOULD, 1966). Among other uses, this approach may allow prediction of quantities that are comparatively difficult to measure, e.g. area of an irregular surface, from others that are quite easy, like body mass or ^a convenient linear dimension. Additionally, departures from geometric similarity with changing size became readily apparent and quantifiable; such information can in turn suggest functional reasons for or consequences of trends in body shape (e.g. GREENEWALT, 1960, 1962, 1975).

This paper presents dimensional data for males of ²⁹ species of Anisoptera from the eastern United States. These are believed to be representative of Nearctic dragonflies and probably of male Anisoptera generally, inasmuch as all families are represented. The dimensionsselected forcomparison reflect my interests in heat exchange and flight energetics, but include those ¹ considered most generally useful in describing dragonfly size and shape.

MATERIALAND METHODS

All specimens were collected as adults and measured within one day of capture except for Tachopleryx thoreyi and Cordulegaster sayi, which were mailed alive from the site of capture and measured about three days after collection. All individuals were obtained at sites in central or southern New Jersey, USA, except the following: T. thoreyi, C. sayi, Macromia georgina, 4 of 5 M. taeniolata, Nasiaeschna pentacantha, and 2 of 4 Tramea carolina, all from Alachua Co., FL; 1 of 5 M. taeniolata and 1 of 3 Epicordulia princeps, Roane Co., TN. I made no attempt to analyze geographic variation.

Mass (M), thoracic mass (M_t) and wing mass (M_w) were measured with an Ainsworth 24N analytical balance (max. sensitivity 0.01 mg), thoracic diameter in the frontal plane (D_t) to the nearest 0.01 cm with a vernier caliper, and wing length (Lw) to the nearest 0.05 cm with ^a millimeter ruler. ¹ painted excised wings with opaque paint and measured their area (Aw) to 0.1 cm² with ^a LiCor Area Meter (mean of three readings). Wing loading (WL) was with a LiCor Area meter (mean of three readings). Wing loading (WL) was calculated as $M \div Aw$, disc loading (DL) was calculated as $M \div \pi r^2$, where $r =$ the mean of forewing (Lfw) and hind wing (Lhw) lengths. Moment of inertia of the wings (Iw) was determined for selected specimens by strip analysis (NORBERG, 1972), using five strips of approximately equal width for each wing.

Data on aspect ratio ($Lw^2 \div Aw$) of individual wings and on approximate area, length and chord (measured at the nodus) of most North American genera were obtained by photocopying wing photographs from NEEDHAM & WESTFALL (1955), measuring length, chord and area with ruler and LiCor Area Meter, respectively, then reducing to approximate true dimensions by assuming that the actual hind wing length was equal to the mid-point of the range given by Needham & Westfall.

Finally, surface area (At), total volume (Vt) and muscle volume (Vm) were determined for isolated thoraxes of single individuals of four species. Thoraxes were dissected from live specimens and fixed for one week in Kahle's solution(50 parts 95% ETOH: ¹⁰ formalin: ⁵ acetic acid: ³⁵ distilled water). Preliminary tests revealed no perceptible shrinkage or swelling of muscle tissue in this fixative. The thoraxes were stored in 70% ETOH for up to four months, then dehydrated and embedded in celloiden. Thick sections (0.25 -0.5 mm) were cut, then photographed or drawn using ^a camera lucida. The perimeter of each slice was measured with ^a cartographers wheel and the total area and area occupied by muscle with ^a planimeter; dimensions were reduced by an appropriate magnification factor determined with a stage micrometer. The corresponding surface areas and volumes of each section or muscle within ^a section were calculated by assuming that each was ^a frustum of a cone with the measured anterior and posterior perimeters and end areas and height equal to section thickness. The anterior end section, however, was treated as ^a segment of ^a sphere. Areas and volumes for each section were summed to give total areas and volumes for the whole thorax.

Regression analyses used an SAS General Linear Models Procedure. Statistical differences are considered significant at the $p = 0.05$ level unless otherwise stated.

RESULTS

The main results are summarized in Tables I-I1I. These give regression statistics for several body and wing dimensions as a function of M and Lhw (Lfw $=$ Lhw $+$ 3-5% for all dragonflies, $r^2 = 0.998$). The independent variables were chosen because they are measured easily and unambiguously and in most cases they were the best predictors of other variables (Mt and Dt were also tried as independent variables). In addition, the full data for selected regressions are shown in Figures 1-4.

In Table ^I the regression coefficients are compared to those expected in geometrically similar organisms. Several significant departures from predicted values occur. The relationships of D_t to M and M_t to D_t both suggest

Independent variable	Dependent variable	Slope	Intercept	\mathbf{r}^2	N	Expected slope	
м	Mt	1.015	-0.278	0.987	107	1.000	
	Dι	$0.405*$	-0.020	0.973	109	0.333	
	Lhw	0.355	0.719	0.918	111	0.333	
	Aw	0.615	1.357	0.882	107	0.667	
	Mw	1.026	1.661	0.972	107	1.000	
	WL	0.384	-1.358	0.747	107	0.333	
	DL	0.296	-1.944	0.664	LO5	0.333	
Lhw	M	$2.586*$	-1.904	0.918	111	3.000	
	Mt	$2.614*$	-2.208	0.904	107	3.000	
	Dt	1.063	-0.799	0.917	109	1.000	
	۸w	$1.749*$	0.104	0.980	107	2.000	
	Mw	$2.755*$	-0.345	0.962	107	3.000	
	WL	0.833	-2.006	0.483	107	1.000	
	DL	0.605	-2.424	0.380	105	1.000	
Dι	Mt	$2.442*$	-0.245	0.967	105	3.000	

Table ¹

Coefficients of the allometric equations showing the relationships among various dimensions of dragonflies

•Slopes differ significantly from expected values.

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Table II

Coefficients of allometric equations showing relationships among dimensions of dragonflies,

by family

• For each dependent variable, categories sharing the same superscript do not differ significantly in adjusted mean square of the dependent variable.

** Slopes differ significantly among families.

that thoracic diameter (and presumably thoracic volume) increases more rapidly than expected with mass. Also, M, Mt, Aw and Mw all increase less rapidly than Lhw, i.e. larger dragonflies have relatively longer, narrower wings.

Table II indicates dimensional differences among the major families investigated. Data for Cordulegastridae, Macromiidae, and Petaluridae are not included in this table because insufficient material was available for statistical analysis. However, some data on these families appear in Figures 1-4. The most consistent interfamilial difference is that Gomphidae tend to have small Lhw and Aw for ^a given M, thus high WL and DL. The sample of gomphids was small and did not cover the full range of size of the family, however, and included mainly *Gomphus*. Generalizations about the family therefore must remain tentative. Wing mass is small in relation to total mass in Gomphidae and Corduliidae, but for different reasons; corduliids have wings of normal size but low Mw for their length, while gomphids have short wings that are rather massive for their length. Mt makes up ^a varying fraction of M in different families, with aeshnids having a relatively low M_t , corduliids and gomphids somewhat larger Mt, and libellulids relatively the largest. The variation with size (slope) of the various dimensions is mostly similar from family to family (except for Dt) and also similar to variation within the suborder as a whole (Tab. I).

Several species or species groups are noteworthy. The libellulid, *Plathemis* lydia, resembles gomphids in that it has small wings for its mass $(Aw = 77\%$ of expected value from Tab. I) and high Mw relative to Lhw (149% of expected value). The ratio of M_t/M is also unusually high. Cordulegaster sayi likewise has unusually small wings ($Aw = 67\%$ of expected value), although in this case Mw is unexceptional. At the other end of the scale, trameine libellulids (*Tramea* and *Pantala*) have longer and broader wings (Lhw $= 116\%$ expected, $Aw = 145\%$ expected) than most dragonflies of similar mass, as do the aeshnids *Boyeria* (Lhw = 120% expected, Aw = 138%) expected) and, to a somewhat lesser extent, Nasiaeschna (Lhw = 116%) expected, $Aw = 124\%$ expected).

Table III compares dragonflies that differ in habit of flight, i.e. that are either ''perchers" or ''fliers" (CORBET, 1963; MAY, 1976); fliers remain on the wing during most of their active period and often glide, while perchers alternately perch and engage in relatively short flights. Of the species considered here, all gomphids and libellulids except the Trameinae are perchers; C. sayi is considered a percher on the basis of its behavior away from breeding sites, but many male Cordulegaster act as fliers when patrolling a territory. Aeshnids, corduliids, macromiids, and trameine libellulids are all fliers. Fliers and perchers differ in the magnitude of most dimensions relative to M or Lhw. Generally fliers of ^a given M have longer wings with greater Aw than comparable perchers. Mw for ^a given Lhw is smaller in fliers, however. Fliers also have smaller Mt/M than perchers (largely because of the high M_t of libellulid perchers). Moreover, fliers tend to have a distinctly larger Dt over the entire range of Mt.

Data based on wing photographs from NEEDHAM & WESTFALL (1955) are consistent with those on real wings. From the former source, log Aw = 1.823 log Lhw + 0.0748, $r^2 = 0.960$, $n = 64$ (cf. Tab. 1). Also, aspect ratio (AR) increases with wing length in both forewings and hindwings: log ARfw = $0.190 \log L$ hw + 0.596 , $r^2 = 0.517$, $n = 64$;

 $log ARhw = 0.220 log Lhw + 0.455, r^2 = 0.478, n = 64.$

Both correlations are significant, although in geometrically similar organisms no significant correlation would be expected. Aspect ratio can also be conveniently calculated as the ratio of wing length to wing chord (Cw) at nodus: $ARf_w = (1.183 \pm 0.0305 \text{ S.D.}) \text{Lfw/Cfw}$; $ARhw = (1.150 \pm 0.0305 \text{ S.D.}) \text{Lfw/Cfw}$; $ARfw = (1.150 \pm 0.0305 \text{ S.D.}) \text{Lfw/Cfw}$; 0.0607)Lhw/ Chw.

Figure ⁵ shows the relation of total wing moment of inertia (Iw) to Lhw.

Table III

Coefficients of allometric equations showing relationships among dimensions of dragonflies, by activity type (flier vs. percher - see text)

• For each dependent variable, categories sharing the same superscript do not differ significantly in adjusted mean square of the dependent variable.

*• Slopes differ significantly between activity habits.

This plot includes data from one female Epiaeschna heros; all other specimens were males. The correlation is quite high, but the slope is significantly less than that expected for geometrically similar insects (i.e., 5.00). This is in accord with the results given above showing that Mw increases only as Lhw^{2,76}. The most marked deviations from the regression occur in Tetra goneuria cynosura, which, like many corduliids, has very light wings, and Tramea carolina, in which mass is concentrated basally because of the expanded anal region of the hind wings. WEIS-FOGH (1973) proposed that for insects in general the moment of inertiaof ^a wing could be predicted from the formula $Iw = 1/6$ MwLw². For dragonflies a regression of Iw on MwLw² gives $I_w = 0.218$ MwLw² - 0.0091 , $r^2 = 0.998$. Thus Weis-Fogh's equation holds if the coefficient is changed to about 1/5, but the relationship only slightly increases accuracy of predicting Iw, at least in this limited sample of fairly similar insects.

The values of M, Mt, Dt, At, Vt and Vm for males of four species appear in Table IV. The sample is too small to attach much significance to any supposed allometry but preliminary equations are: log $At = 1.75$ log $Dt +$ 0.69, $r^2 = 0.978$; log Vt = 2.89 log Dt - 0.060, $r^2 = 0.986$. Alternative expressions, of equal predictive value and possibly more convenient as rules of thumb are: At = 5.10 Dt² + 0.132, $r^2 = 0.985$; Vt = 0.978 Dt³ - 0.020, $r^2 =$ 0.989; i.e. to a first approximation $St = 5 Dt^2$ and $Vt = Dt^3$.

Density of the thorax (Mt/Vt) is lower in the aeshnid fliers (*Boyeria* and Anax) than in the libellulid perchers and within each of those groups appears to decrease with increasing size. Likewise, the proportion of the thorax that is filled with muscle (V_m/V_t) is lower in the aeshnids and also decreases with increasing size. As expected, At/Vt decreases markedly with increasing size.

Species	м (g)	M.t (g)	Dt* (cm)	St (cm ²)	٧t (cm ³)	Vm (cm)	Mt/Vt	V_m/V_t	St/Vt (cut')
Pachydiplax longipennis 0.156		0.087	0.45	1.26	0.092	0.058	0.948	0.627	13.7
Libellula incesta	0.377	0.241	0.69	2.60	0.285	0.172	0.846	0.603	9.1
Boyeria vinosa	0.395	0.177	0.64	2.03	0.216	0.102	0.819	0.472	9.4
Anax junius	1.090	0.415	0.84	3.79	0.575	0.232	0.722	0.403	6.6

Table IV

Relationships among mass and thoracic dimensions in four individual dragonflies

* Measured from drawings of sections.

Fig. 1. Thoracic mass (Mt) as ^a function of total mass (M) in male Anisoptera. Solid line is least squares regression of log Mt on log M. Dashed line indicates slope expected for geo-metrically similar organisms (intercept of this line is arbitrary). Symbols: \bullet -Libellulidae, o - Aeshnidae, n - Corduliidae, A -Gomphidae, x - Macromiidae, \Diamond - Cordulegasteridae, ∇ -Petaluridae.

Fig. 2. Total mass (M) as a function of hindwing length (Lhw) in maleAnisoptera. Symbols as in Fig. I.

DISCUSSION

An important reason for presenting the equations of Tables 1-II1 is to make possible estimation of several dimensions from others more easily measured. For example, approximate body mass of the living insect can be calculated from wing length of ^a dried specimen. Another potential utility of such regressions lies in the light they may shed on the nature of adaptive changes in shape with variation in size and of departures from predicted dimensions(GOULD, 1966, 1975; SMITH, 1980). The following discussion represents an attempt to elucidate some of these adaptations.

WING PROPORTIONS

One of the most consistent allometric trends revealed by these data is that toward relatively longer (Fig. 2) and narrower, hence lighter, wings with increasing body size. Relationships of M, Aw, AR, and Iw to Lhw all reinforce this conclusion. Sphingid and saturniid moths exhibit somewhat similar allometry (BAR-THOLOMEW & CASEY, 1978). GREENEWALTs (1962) extensive data for the entire spectrum of flying animals shows ^a slight trend toward relatively longer wings at high body mass, but little apparent departure from geometrics similarity in the relation of Aw to Lw. In insects as a group there is, if anything, ^a trend toward disproportionately high area as wings lengthen, mainly because butterflies and large moths have long and very broad wings.

The functional significance of long, narrow wings in large dragonflies is not certain, but several benefits to flight performance can be suggested. In general the energy required for flight, relative to energy available (i.e. maximum metabolism), is greater in larger flying animals (PENNYCUICK, 1969). Thus large dragonflies may be, to ^a greater extent thansmall species, under selective pressure to minimize energy expenditure in flight. This could be especially true since the flight muscle mass of large species may be relatively less than in small species (see below). Long, narrow wings increase the area swept by the moving wing (wing disc area; PENNYCUICK, 1969) and probably increase lift coefficient and lift-to-drag ratio (see, e.g. OLSON, 1961) while at the same time minimizing wing mass. The latter results in decreased Iw, and therefore reduced inertial power losses (WEIS--FOGH, 1973), and possibly increased wingbeat frequency(GREENEWALT, 1960). GREENEWALT (1975) showed that for birds minimum mass- -specific power requirements for flight increase with mass and wing area but decrease with increasing wing length, at least in part for the reasons cited above. Cost of transport also decreases with wing length but increases with area. Thus lengthening Lhw while minimizing Aw should be increasingly advantageous as power requirements increase. The fact that fliers have relatively longer wings than perchers is consistent with this suggestion since fliers must, of course, sustain flight for longer periods.

GREENEWALT (1975) also demonstrated that the speed at which power output is minimal increases with mass but decreases with both wing area and length. Since the necessity to maintain high speed must limit maneuverability, large dragonflies that fly for long periods in situations where space is limited should ideally have long, broad wings. Boyeria patrols among roots and overhangs along small streams, often in dim light, and it is characterized by unusually long, broad wings; so, to ^a lesser extent, is Nasiaeschna, another flier of wooded streams and swamps. Another notable example are members of the tropical, forest-dwelling genus Gynacantha (May, unpublished data).

Another important wing characteristic is strength. A structure subject to buckling stress should increase in thickness relative to its length as the latter increases (McMAHON, 1973), in order to maintain comparable strength. This generally means that mass should increase proportionally faster than L³. Just such a relationship is found in weight-bearing bones (PRANGE, et al., 1979) and in the wings of flying animals generally

Fig. 3. Wing mass (Mw) as ^a function of hindwing length (Lhw) in male Anisoptera. Symbols as in Fig. 1.

Fig. 4. Thoracic mass (Mt) as ^a function of thoracic diameter (Dt) in male Anisoptera. Symbols as in Fig. I.

(GREENEWALT, 1962). It is not seen in Anisoptera (Tab. II), but the picture here is confounded by the proportionate decrease in wing area. In fact, M_w/A_w^{α} Lhw¹¹⁶ in perchers and Lhw¹¹⁸ in fliers, suggesting that thickness does increase disproportionately relative to length; the ratio should increase as Lhw¹⁰ in dimensionally similar animals.

Perchers have higher wing mass for ^a given Lhw than do fliers (Fig. 3), and some perchers that habitually rest on the ground (Gomphidae and Plathemis) have the greatest relative wing mass. This suggests that frequent, sudden take-offs, especially when wing movement may be restricted or wings may strike the substrate on the first stroke, may require greater wing rigidity than does sustained flight. It should be noted, however, that ground-perching Erythemis do not have especially massive wings and that Cordulegaster sayi, which has massive wings (for their length), does not perch on the ground.

THORACIC PROPORTIONS

Although Vt probably increases approximately with Dt^3 , Mt increases only with

 Dt^{24} (Fig. 4). In addition, fliers tend to have relatively less massive thoraxes $(Fig. 1)$ and lower Vm/Vt than perchers. These characteristics are all probably related to parallel differences in heat exchange and possible also power requirements for flight.

In all Anisoptera the thoracic musculature is largely surrounded by subcuticular air sacs that provide substantial insulation to the flight muscles; the degree of insulation is greatest in large species, especially large fliers (CHURCH, 1960; MAY, 1976, 1978). In very small species, the ratio of thoracic surface to volume (Tab. IV) may be so high that no amount of

Fig. 5. Moment of inertia of all four wings (Iw) as ^a function of hindwing length (Lhw) in Anisoptera: (I) Perithemis tenera, — (2) Gomphus exilis, — (3) Tetragoneuria cynosura, - (4) Pachydiplax longipennis, $-$ (5) Basiaeschna janata, $-$ (6) Cordulegaster sayi, $-$ — (3) Basiaescnna janaia, — (6) Corauiegasier sayi, —
(7) Libellula pulchella, — (8) Boyeria vinosa, — (9) Tramea carolina, - (10) Tachopteryx thoreyi, - (11) Anax junius, - (12) Macromia taeniolata, - (13) Epiaeschna heros. Symbols as in Fig. I.

insulation can greatly retard heat exchange, while in larger dragonflies a significant insulating effect, and thus selection for increased insulation, is possible. In addition, since fliers generally are endotherms(MAY, 1976), good insulation to prevent excessive heat loss during flight probably is of greater selective advantage than in largely ectothermic perchers. The characteristics listed at the beginning of this section are all due to the relative increase in the peripheral air space in large dragonflies, especially large fliers. In the sections used to determine Vi and Vm it was impossible to distinguish air spaces from haemocoel, but the reduction in thor-

acic density in parallel with reduced V_m/Vt tends to confirm that the latter was due mainly to an increase in air sac volume.

¹ did not measure directly the relative mass of dragonfly flight muscle, but if its density is about 1.06 g.cm³ (data for frog muscle; SPECTOR, 1956), then from Table IV the tissue should be about 25% of M in fliers and about 45% in perchers. These percentages are about the same as found by MAGNAN & PERRILL1AT-BOTONET (1932) for fliers but much higher than their figures for perchers. The reduced relative muscle mass of fliers, especially aeshnids, could indicate that maximum short-term power requirements are usually less for species characterized by sustained flight than for those that typically make repeated sudden takeoffs.

REFERENCES

- BARTHOLOMEW, G.A. & T.M. CASEY, 1978. Oxygen consumption of moths during rest, pre-flight warm-up, and flight in relation to body size and wing morphology. J. exp. Biol. 76; 11-25.
- CHURCH, N.S., 1960, Heat loss and the body temperature of flying insects. J. exp. Biol. 37: 186-212.
- CORBET, P.S., 1963. A biology of dragonflies. Quadrangle Books, Chicago.
- GOULD, S.J., 1966. Allometry and size in ontogeny and phylogeny. Biol. Rev. 41: 587-640.
- GOULD, S.J., 1975. On the scaling of tooth size in mammals. Am. Zool. 15: 351-362.
- GREENEWALT, C.H., 1960. The wings of insects and birds as mechanical oscillators. Proc. Am. phil. Soc. 104: 605-611.
- GREENEWALT, C.H., 1962. Dimensional relationships for flying animals. Smithson. mise. Colins 144: 1-46.
- GREENEWALT, C.H., 1975, The flight of birds. The significant dimensions, their departure from the requirements for dimensional similarity and the effect on flight aerodynamics of that departure. Trans. Am. phil. Soc. 65: 5-67.
- HUXLEY, J.S., 1932. Problems of relative growth. MacVeagh, London.
- MAGNAN, A. & C. PERR1LLIAT-BOTONET, 1932. Sur le poidsrelatif des muscles moteurs des ailes chez les insectes. C.r. Acad. Sei. 195: 559-561. [cited in Greenewalt, 1962].
- MAY, M.L., 1976. Thermoregulation and adaptation to temperature in dragonflies (Odonata: Anisoptera). Ecol. Monogr. 64: 1-32.
- MAY, M.L., 1978. Thermal adaptations of dragonflies. Odonatologica 7: 27-47.
- McMAHON, T., 1973. Size and shape in biology. Science 179: 1201-1204.
- NEEDHAM, J.G. & M.J. WESTFALL, 1955. A manual of the dragonflies of North America (Anisoptera). Univ. California Press, Berkeley.
- NORBERG, R.A., 1975. Hovering flight of the dragonfly Aeschna juncea L., kinematics and aerodynamics. In: T.Y.-T. Wu, C.J. Brokaw & C. Brennen, [Eds], Swimming and flying in nature, vol. 2, pp. 763-781. Plenum, New York.
- OLSON, R.M., 1961. Essentials of engineering fluid mechanics. Int. Textbook Co., Scranton, Pa.
- PENNYCUICK, C.J., 1969. The mechanics of bird migration. Ibis 111: 525-556.
- PRANGE, H.D., J.F. ANDERSON & H. RAHN, 1979. Scaling of skeletal mass to body mass in birds and mammals. Am. Naturalist 113: 103-122.
- SMITH, R.J., 1980. Rethinking allometry. J. theor. Biol. 87: 97-111.
- SPECTOR, W.S., [Ed.], 1956. Handbook of biological data. Saunders, Philadelphia.
- WEIS-FOGH, T., 1973. Quick estimates of flight fitness in hovering animals, including novel mechanisms for lift production. J. exp. Biol. 59: 169-230.